Name:

Date:__

 $m_{AB} = \frac{8-4}{3-1} = 2$

 $m_{CD} = \frac{-2-2}{1-3} = 2$

 $m_{AB} = m_{CD}$

AB || CD

Expressing Properties: Coordinate Proofs

We can use coordinates to prove simple geometric theorems algebraically by using simple coordinate algebra. The formulas we will use are:

Distance formula:
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Slope formula: $m = \frac{y_2 - y_1}{x_2 - x_1}$

Example: Without graphing, determine whether points A(1,4), B(3,8), C(3,2), and D(1,-2) form rectangle ABCD.

Step 1: Find the slope of two sides of the figure. A slope is a measure of the rise/fall of a line on a coordinate plane. As a result, parallel lines have the same slope.

Step 2: Identify whether the sides of ABCD intersect at 90° angles. In order for an object to be a square, it must contain two sets of parallel lines that intersect at 90 degree angles. Coordinates that intersect at 90 degrees are considered perpendicular. $m_{AB} = \frac{8 - 4}{3 - 1} = 2$ $m_{BC} = \frac{2 - 8}{3 - 3} = undefined$ (vertical line)

Perpendicular lines have slopes that are complete reciprocals both in sign (+/-) and placement. In order to be completely reciprocal to mAB, mBC would have to be $-\frac{1}{2}$. mBC $\neq -\frac{1}{2}$; therefore ABCD is not a rectangle.

Example: Use the given coordinates to find the midpoint of segment AB. Then, determine the perimeter and area of $\triangle ACD$.

Step 1: Determine the length of AB/2. Midpt = 2 **Step 2:** Calculate the length of AC, CD, and DA

$$d = \sqrt{\frac{(x_2 - x_1)^2 + (y_2 - y_1)^2}{(4 - 1)^2 + (6 - 2)^2}}$$

$$d_{AC} = \sqrt{\frac{(4 - 1)^2 + (6 - 2)^2}{(1 - 7)^2 + (2 - 2)^2}}$$

$$AC = 5$$

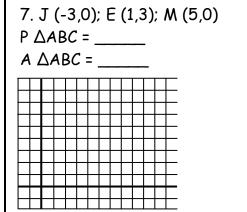
$$CD = 6$$

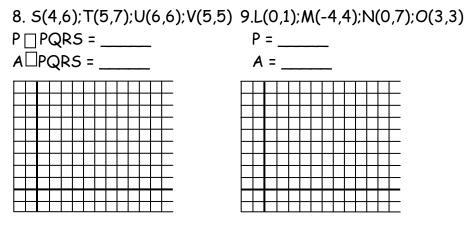
$$AD = 5$$

$$d_{AD} = \sqrt{\frac{(4 - 7)^2 + (6 - 2)^2}{(4 - 7)^2 + (6 - 2)^2}}$$

Step 3: Calculate the Perimeter and Area of $\triangle ACD$. P = s1 + s2 + s3 = AC + CD + AD = 5 + 6 + 5 = 16 A = $\frac{1}{2}$ Bh = $(\frac{1}{2})(6)(4) = 12$

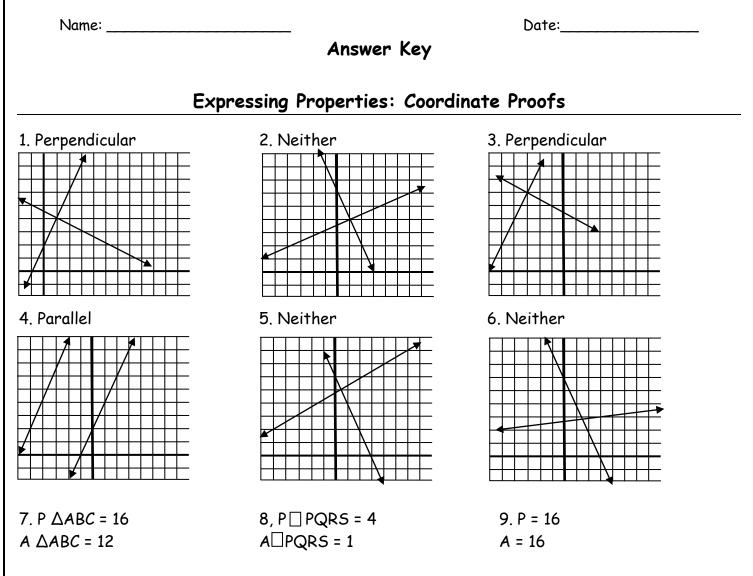
Name: Date: Practice. Identify whether the following segments are parallel, perpendicular, or neither. Graph. A (3, 3) B (-5, 2) C (1, 4) D (2, 6) E (3, 0) F (-6, 0) 1. AC and DC 2. BD and CE 3. BF and AC 4. CD and BF 5. BD and CE 6. AB and CE Use the distance formula to determine the perimeter and area of each of the following objects.





10. The triangle midsegment theorem states that a midsegment of a triangle is parallel to a side of the triangle, and its length is half the length of that side. Using distance formula, calculate the coordinates of each midsegment point of Δ KTM: K(-5,6) T(1,2) M(-7,2).

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10. The coordinates of the midsegment triangle are (-2,4), (-3,2), and (-6,4).